2.2: The Derivative Function

Definition: For a function f, we define the **derivative function**, f', by f'(x) = Instantaneous rate of change of f at $x = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$.



Exercise 1: Match each of the two graphs below to one of the derivative graphs above.



Exercise 2: Draw a possible graph of y = f(x) given the following information about its derivative.

- 1. f'(x) > 0 for x < -1
- 2. f'(x) < 0 for x > -1

3.
$$f'(x) = 0$$
 for $x = -1$

Exercise 3: A vehicle moving along a straight road has distance f(t) from its starting point at time t. Which of the graphs below could be f'(t) for the following scenarios?

- 1. A bus on a popuar route, with no traffic
- 2. A car with no traffic and all green lights
- 3. A car in heavy traffic conditions



Exercise 4: Sketch the derivative of the function f(x) given below.



Exercise 5: Sketch the derivative of the function f(x) given below.

